

# ТЕОРЕТИЧЕСКОЕ ИССЛЕДОВАНИЕ КИНЕТИКИ ДИМЕРИЗАЦИИ ОКСИДА АЛЮМИНИЯ\*

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**Аннотация:** Исследована реакция димеризации оксида алюминия методами квантовой химии. С помощью гибридного функционала электронной плотности с коррекцией по теории возмущений второго порядка B2PLYP построена соответствующая поверхность потенциальной энергии (ППЭ). Показано, что взаимодействие двух мономеров  $\text{Al}_2\text{O}_3$  даже в простейшем случае приводит к образованию димеров  $(\text{Al}_2\text{O}_3)_2$  в различных изомерных формах. Анализ, основанный на теории Райса–Рамспергера–Касселя–Маркуса (РПКМ), показал, что константа скорости процесса димеризации  $2\text{Al}_2\text{O}_3 \rightarrow (\text{Al}_2\text{O}_3)_2$  может быть на порядки ниже, чем оценка по модели твердых сфер. Зависимость соответствующей константы скорости от температуры и давления в диапазонах  $T = 300\text{--}3000$  К и  $P = 10^{-4}\text{--}10^2$  атм может быть представлена в форме Линдемана следующим образом:  $k_0(T) = 8,01 \cdot 10^{19} T^{-1,079} \exp(21671/T)$  см<sup>6</sup>/(моль<sup>2</sup>с);  $k_\infty(T) = 9,91 \cdot 10^{19} T^{-1,754} \exp(-2911/T)$  см<sup>3</sup>/(моль·с).

**Ключевые слова:** оксид алюминия; димеризация; РПКМ

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# THEORETICAL STUDY OF DIMERIZATION KINETICS OF ALUMINUM OXIDE

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**Abstract:** The study is aimed at the quantum chemical investigation of alumina dimerization. The appropriate potential energy surface is explored using the hybrid density functional with perturbative second-order correlation B2PLYP. It is shown that the interaction of two  $\text{Al}_2\text{O}_3$  monomers leads to  $(\text{Al}_2\text{O}_3)_2$  formation in different forms. The RRKM-based analysis revealed that the rate constant of  $2\text{Al}_2\text{O}_3 \rightarrow (\text{Al}_2\text{O}_3)_2$  process can be lower by several orders of magnitude than the estimates by the rigid-sphere theory. The corresponding temperature- and pressure-dependent rate constant can be expressed by the Lindemann fit as follows:  $k_0(T) = 8.01 \cdot 10^{19} T^{-1.079} \exp(21671/T) \text{ cm}^6/(\text{mole}^2\text{s})$  and  $k_\infty(T) = 9.91 \cdot 10^{19} T^{-1.754} \exp(-2911/T) \text{ cm}^3/(\text{mole}\cdot\text{s})$ .

**Keywords:** alumina; dimerization; RRKM

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